

Analysis of the Fluorescence Spectrum of $\text{LiYF}_4:\text{Eu}^{3+}$

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Abstract

The fluorescence spectrum of the scheelite-type $\text{LiYF}_4/\text{Eu}^{3+}$ crystal was analyzed and accurately described by a set of crystal field parameters in a S_4 – not far from D_{2d} – symmetry.

Introduction

Compounds with Scheelite-like structure have in the past been the subject of many spectroscopic investigations, as well as *ab initio* calculations [1]. LiYF_4 has been studied as a promising efficient laser when doped by various rare earths, mainly by Nd^{3+} . A complete survey of the actual results is found in reference [2].

The symmetry of the point site, S_4 – not far from D_{2d} –, constitutes a sensitive case where various magneto-optical features can be precisely studied, due to the relatively small number of phenomenological parameters involved. This work was performed in order to characterize the optical properties of a single crystal of $\text{LiYF}_4:\text{Eu}^{3+}$.

From the fluorescence spectrum the crystal field parameters (c.f.p.) were calculated and the wavefunctions were derived in view of a future precise simulation of the magnetic circular dichroism (MCD) [3, 4] spectra.

Experimental

Preparation and Structure of the $\text{LiYF}_4/\text{Eu}^{3+}$ Compound

Method of synthesis

Crystals of LiYF_4 , doped with Eu^{3+} , were grown by spontaneous nucleation in the melt [5].

As starting materials, high purity LiF and EuF_3 (99.99%), and anhydrous YF_3 (99.9999%) were used. According to the mole weight relations between YF_3 and EuF_3 , the doping concentration of the $\text{LiYF}_4:\text{Eu}^{3+}$ crystals is $5.00 \pm 0.05\%$.

By indirect cooling of the crucible bottom, the temperature gradient in the melt was increased during the growth, thereby improving size and quality of crystals.

Possible contaminations of the melt are LiF , YF_3 , EuF_3 , YOF and EuOF . However, analysis of the melt by Debye-Scherrer exposures and polarized light microscope did not reveal any foreign phases. Furthermore, the transparency of the sample indicates a high purity, because even small amounts of wrong phases (10 ppm) would lead to severe decrease of optical transmission.

For the rare earths (Ln^{3+}), the yttrium-ion will be substituted, partially or wholly, by a lanthanide ion.

Due to a destructive $\text{Ln}^{3+}-\text{Ln}^{3+}$ interaction, the doping percentage may not exceed 5% for the case of Eu^{3+} , if growth of large, perfect crystals is wanted.

Structure [11]

The LiYF_4 crystals are uniaxial hosts, belonging to the tetragonal scheelite structure (space group C_{4h}^6).

The polyhedron, formed by the nearest surroundings of the rare earth ions, eight fluorides (F^-), is nearly a dodecahedron.

The crystallographic point site symmetry is D_{2d} , slightly distorted to a S_4 -symmetry; this implies a distortion of the ϕ coordinates from the dodecahedron D_{2d} values [6].

Spectroscopic Measurements

The fluorescence of the $\text{LiYF}_4:5\% \text{Eu}^{3+}$ was excited by an ORIEL 200 W mercury lamp, equipped

TABLE I. Selection Rules for Electric and Magnetic Dipole Transitions (in Kosters and Cottons Notation).

| $D_{2d_{E,D}}$ | $\Gamma_1(A_1)$ | $\Gamma_2(A_2)$ | $\Gamma_3(B_1)$ | $\Gamma_4(B_2)$ | $\Gamma_5(E)$ | $D_{2d_{M,D}}$ | Γ_1 | Γ_2 | Γ_3 | Γ_4 | Γ_5 |
|----------------|-----------------|-----------------|-------------------|-----------------|---------------|----------------|------------|------------|----------------|------------|------------|
| Γ_1 | — | — | — | π | σ | Γ_1 | — | σ | — | — | π |
| Γ_2 | — | — | π | — | σ | Γ_2 | σ | — | — | — | π |
| Γ_3 | — | π | — | — | σ | Γ_3 | — | — | — | σ | π |
| Γ_4 | π | — | — | — | σ | Γ_4 | — | — | σ | — | π |
| Γ_5 | σ | σ | σ | σ | π | Γ_5 | π | π | π | π | σ |
| $S_{4_{E,D}}$ | $\Gamma_1(A)$ | $\Gamma_2(B)$ | $\Gamma_{3,4}(E)$ | | | $S_{4_{M,D}}$ | Γ_1 | Γ_2 | $\Gamma_{3,4}$ | | |
| Γ_1 | — | π | σ | | | Γ_1 | σ | — | π | | |
| Γ_2 | π | — | σ | | | Γ_2 | — | σ | π | | |
| $\Gamma_{3,4}$ | σ | σ | π | | | $\Gamma_{3,4}$ | π | π | σ | | |

with wide band long-UV filters. The UV-light was focussed on the sample, immersed in liquid nitrogen (77 K), and the reflected light entered a 1 m Jarrel-Ash monochromator having a resolution of about 0.1 Å.

Alternatively, to obtain the selective excitation of the 5D_0 -level of Eu^{3+} , a Rhodamin 6 G dye laser coupled to a 4 W Ar-ion laser was used. Because of the fact that the $^5D_0 \rightarrow ^7F_0$ transition is forbidden in the considered symmetry, the selective excitation cannot be performed through this transition. However, when the laser is tuned to the $^5D_0 \rightarrow ^7F_1$ transitions at 77 K, the remaining thermal population of the lowest 7F_1 Stark level ($\pm 0.5\%$) is sufficient to excite $^5D_0 \leftarrow ^7F_1$. The analysed wavelength region varied between 14200 cm^{-1} and 20800 cm^{-1} corresponding to the transitions $^5D_J (J = 0, 1, 2) \rightarrow ^7F_J (J = 0, 1, 2, 3, 4, 5)$ of Eu^{3+} .

Because of the fact that the fluorescence measurements were unpolarised, the orientation of the crystal with respect to the incident light was unimportant. In the present case, the optical axis was lying in the plane of the crystal.

Selection Rules for Transitions

In a crystal the $^{2S+1}L_J$ levels of the Eu^{3+} are split into several Stark sublevels according to their J -value [7].

As from the previous section it appears that a small distortion from D_{2d} to S_4 has to be taken into account, the two symmetries are considered and labels are given accordingly to the Koster [7] and Cotton [8] notations.

In Table I the selection rules for electric and magnetic dipole transitions are summarized.

Analysis of the Fluorescence Spectra

(i) The transitions having different emitting levels towards the same final level appear on the spectrum as a group of peaks which will appear as a same group

of homologous peaks when transition to another final level is considered.

(ii) Although the selection rules give spectra compatible with a S_4 pointgroup, the relative weakness of certain levels suggests that the site symmetry is not far from D_{2d} . This remark is of interest for the simulation of the energy level positions because some irreducible representations differ for the two groups, as well as electronic transition selection rules. For instance the $\Gamma_1(A)$ and $\Gamma_2(B)$ are undifferentiated in S_4 but split respectively into $\Gamma_1(A_1) - \Gamma_2(A_2)$ and $\Gamma_3(B_1) - \Gamma_4(B_2)$ in D_{2d} . This will help for the attribution of the irreducible representation and fix the relative sign of B_4^+ and B_4^- .

Region 19050–19000 cm^{-1} (Fig. 1a) $^5D_1 \rightarrow ^7F_0$

The two peaks correspond to magnetic dipole transitions from Γ_1 and $\Gamma_{3,4}$ (S_4) of 5D_1 to the Γ_1 (S_4) ground state (7F_0) in respectively σ - and π -polarisation. The energy separation between Γ_1 and $\Gamma_{3,4}$ is 21 cm^{-1} .

Region 18800–18500 cm^{-1} and 16950–16800 cm^{-1} (Fig. 1a, 1b) $\rightarrow ^7F_1$

The peaks at 16840 cm^{-1} and 16395 cm^{-1} correspond to the magnetic dipole $^5D_0 \rightarrow ^7F_1$ transition, respectively $\Gamma_1 \rightarrow \Gamma_1$ (S_4) and $\Gamma_1 \rightarrow \Gamma_{3,4}$. The energy separation of 95 cm^{-1} helps to assign the three intense peaks in the region $18800\text{--}18000\text{ cm}^{-1}$. They correspond to the $^5D_1 \rightarrow ^7F_1$ transition, which is both magnetic and electric dipole allowed. The weak shoulder at 18601 cm^{-1} is probably the $\Gamma_1 \rightarrow \Gamma_1$ magnetic dipole σ -transition.

Region 18200–17800 cm^{-1} and 16500–15900 cm^{-1} (Fig. 1a, 1b and 2) $\rightarrow ^7F_2$

This region corresponds respectively to the $^5D_1 \rightarrow ^7F_2$ transition and to a superposition of the $^5D_0 \rightarrow ^7F_2$ and $^5D_1 \rightarrow ^7F_4$ transitions.

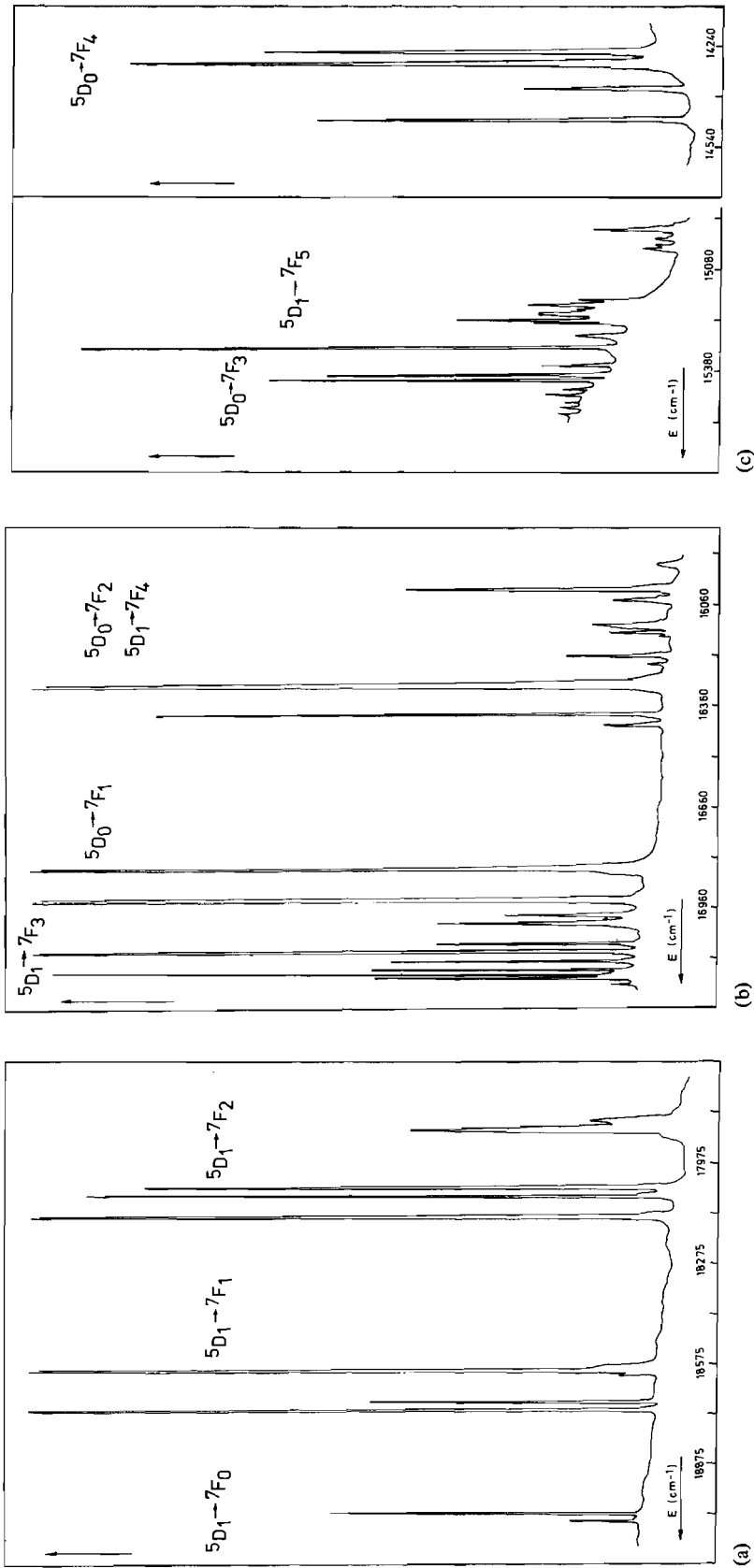


Fig. 1a,b,c. Fluorescence spectra of the $\text{LiYF}_4:\text{Eu}^{3+}$ recorded by excitation with a 200 W Mercury lamp. (The scale in ordinate is arbitrary and varies for each wavelength region).

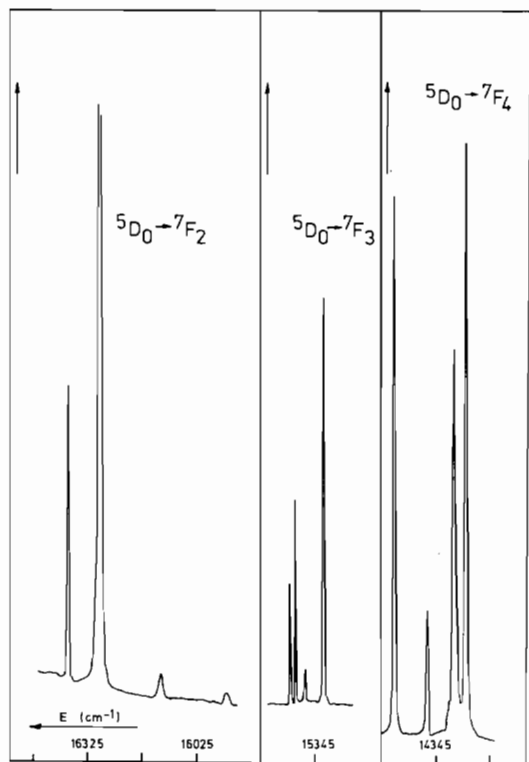


Fig. 2. Fluorescence spectra of the $\text{LiYF}_4/\text{Eu}^{3+}$ for selective excitation of the ${}^5\text{D}_0$ -level by a Rhodamin 6 G dye laser coupled to a 4 W Ar-ion laser. (The scale in ordinate is arbitrary and varies for each wavelength region).

With the laser excitation only the ${}^5\text{D}_0 \rightarrow {}^7\text{F}_2$ is seen, allowing us to identify the components at 16120 cm^{-1} , 16293 cm^{-1} and 16379 cm^{-1} as belonging to this transition. The weak peak at 16120 cm^{-1} can be unambiguously associated to the $\Gamma_1 \rightarrow \Gamma_2$ Stark component, because this transition is due to the slight distortion from D_{2d} to S_4 ($\Gamma_1 \rightarrow \Gamma_3$ is electric-dipole forbidden in D_{2d}). The weak signal at 15938 cm^{-1} probably has its origin in a vibronic transition mechanism (associated with ${}^5\text{D}_0 \rightarrow {}^7\text{F}_2$: $\bar{\nu} \approx 350\text{ cm}^{-1}$).

The ${}^5\text{D}_1 \rightarrow {}^7\text{F}_2$ (Fig. 2a) helps to assign the two remaining peaks in providing the possibility to position the Γ_1 level belonging to ${}^7\text{F}_2$ at 1172 cm^{-1} above the groundstate. Indeed, in the region 17800 cm^{-1} – 18200 cm^{-1} the twins can be associated with the magnetic dipole transition from the Γ_1 and $\Gamma_{3,4}$ levels of ${}^5\text{D}_1$ to the Γ_2 and $\Gamma_{3,4}$ levels of ${}^7\text{F}_2$. The fifth peak at 18129 cm^{-1} corresponds to the $\Gamma_{3,4}$ to Γ_2 while the expected second $\Gamma_{3,4} \rightarrow \Gamma_2$ transition is superposed on the $\Gamma_1 \rightarrow \Gamma_1$ transition.

The 17891 cm^{-1} peak could be the weakly allowed electric dipole transition $\Gamma_1 \rightarrow \Gamma_2$.

Region 17200 – 16950 cm^{-1} and 15420 – 15320 cm^{-1} (Fig. 1b, 1c and 2) $\rightarrow {}^7\text{F}_3$

This region corresponds to the ${}^5\text{D}_1 \rightarrow {}^7\text{F}_3$ and ${}^5\text{D}_0 \rightarrow {}^7\text{F}_3$ fluorescence. The Stark splitting of the ${}^7\text{F}_3$ level occurs following Γ_1 , $2\Gamma_2$ and $2\Gamma_{3,4}$ in S_4 and Γ_1 , Γ_3 and $2\Gamma_5$ in D_{2d} .

From the ${}^5\text{D}_0$ (Γ_1), transitions will be both electric and magnetic dipole allowed.

If in first approximation only the D_{2d} -symmetry is considered, four kinds of possibilities occur, namely from Γ_1 to Γ_2 , Γ_4 and Γ_5 ($2\times$). This is found experimentally, leading to the positions at 15317 cm^{-1} (Γ_2), 15367 cm^{-1} (Γ_4), 15397 cm^{-1} (Γ_5) and 15411 cm^{-1} (Γ_5).

Remaining transitions, due to the slight distortion to S_4 , are hardly seen and will be weakly allowed.

Concerning the ${}^5\text{D}_1 \rightarrow {}^7\text{F}_3$, the expectations for an electric dipole transition are: from Γ_2 to Γ_3 and Γ_5 ($2\times$), and from Γ_5 to all Γ_i (Γ_2 , Γ_3 , Γ_4 and $2\times\Gamma_5$).

Experimentally there are two groups of three peaks, separated by 21 cm^{-1} , which would correspond to the electric dipole transitions Γ_2 to Γ_3 and Γ_5 ($2\times$) in D_{2d} . Besides, the two lone peaks can be associated with the transition from Γ_5 to Γ_4 and Γ_2 .

If it is assumed that the transitions have mainly an electric dipole character, the distortion to S_4 would allow to some extent the $\Gamma_1 \rightarrow \Gamma_2$ which is forbidden in D_{2d} ($\Gamma_2 \rightarrow \Gamma_4$).

Region 14200 – 14500 cm^{-1} and 15900 – 16500 cm^{-1} (Fig. 1b, 1c and 2) $\rightarrow {}^7\text{F}_4$

The region 15900 cm^{-1} – 16500 cm^{-1} corresponds to a superposition of ${}^5\text{D}_1 \rightarrow {}^7\text{F}_4$ and ${}^5\text{D}_0 \rightarrow {}^7\text{F}_2$; with laser excitation, one obtains the identification of the four peaks of the ${}^5\text{D}_0 \rightarrow {}^7\text{F}_2$ transition. The remaining nine signals give the emission from the ${}^5\text{D}_1$ level.

The Stark splitting of the ${}^7\text{F}_4$ multiplet results in $2\times\Gamma_1$, Γ_2 , Γ_3 , Γ_4 and $2\times\Gamma_5$ in D_{2d} , and $3\times\Gamma_1$, $2\times\Gamma_2$ and $2\times\Gamma_{3,4}$ in S_4 .

Following the electric dipole transition rules one should obtain three peaks in D_{2d} and four in S_4 for the ${}^5\text{D}_0 \rightarrow {}^7\text{F}_4$ transition. Experimentally, three intense signals and one weak signal are seen. This last one is in agreement with the allowed $\Gamma_1 \rightarrow \Gamma_2$ transition in S_4 (forbidden $\Gamma_1 \rightarrow \Gamma_3$ in D_{2d}).

The differentiation between the Γ_2 and $\Gamma_{3,4}$ representations (in S_4) and the position of the three remaining Γ_1 representations can be made by the interpretation of the ${}^5\text{D}_1 \rightarrow {}^7\text{F}_4$ transition. The spectrum gives three pairs of peaks associated with the Γ_1 and $\Gamma_{3,4}$ to Γ_2 and $\Gamma_{3,4}$ transitions. Two of the three observed lone peaks are characterized as $\Gamma_{3,4} \rightarrow \Gamma_1$ transitions (16149 cm^{-1} and 16413 cm^{-1}).

The signal at 16402 cm^{-1} can be explained by a $\Gamma_{3,4}$ to Γ_2 transition. In theory one should expect

TABLE II. Identification of the Electronic Transitions of $\text{LiYF}_4/\text{Eu}^{3+}$.

| Transition | $\bar{\nu}$ (cm^{-1}) | Polarisation and mechanism | Identification | |
|-------------------------------|----------------------------------|-----------------------------|---|---|
| | | | S_4 | D_{2d} |
| ${}^5D_0 \rightarrow {}^7F_4$ | 14257 | ED σ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_1 \rightarrow \Gamma_5$ |
| | 14291 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_1 \rightarrow \Gamma_4$ |
| | 14365 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_1 \rightarrow \Gamma_3$ |
| | 14458 | ED σ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_1 \rightarrow \Gamma_5$ |
| ${}^5D_1 \rightarrow {}^7F_5$ | 14949 | ED σ | $\Gamma_{3,4} \rightarrow \Gamma_2$ | $\Gamma_5 \rightarrow \Gamma_4$ |
| | 14969 | ED $\pi, \text{ED } \pi$ | $(\Gamma_1 \rightarrow \Gamma_2)/\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $(\Gamma_2 \rightarrow \Gamma_4)/\Gamma_5 \rightarrow \Gamma_5$ |
| | 14982 | ED σ | $\Gamma_{3,4} \rightarrow \Gamma_1$ | $\Gamma_5 \rightarrow \Gamma_1/\Gamma_2$ |
| | 14991 | ED σ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| | 15014 | ED σ | $\Gamma_{3,4} \rightarrow \Gamma_1$ | $\Gamma_5 \rightarrow \Gamma_1/\Gamma_2$ |
| | 15021 | ED π | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| | 15176 | ED σ | $\Gamma_{3,4} \rightarrow \Gamma_1$ | $\Gamma_5 \rightarrow \Gamma_2$ |
| | 15188 | ED σ | | |
| | 15201 | | | |
| | 15212 | ED π | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| | 15224 | ED σ | $\Gamma_{3,4} \rightarrow \Gamma_2$ | $\Gamma_5 \rightarrow \Gamma_3$ |
| | 15234 | ED σ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| | 15245 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_2 \rightarrow \Gamma_3$ |
| | 15282 | | | |
| | ${}^5D_0 \rightarrow {}^7F_3$ | 15317 | ED $\sigma, \text{MD } \pi$ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ |
| 15367 | | MD σ | $\Gamma_1 \rightarrow \Gamma_1$ | $\Gamma_1 \rightarrow \Gamma_2$ |
| 15397 | | ED $\sigma, \text{MD } \pi$ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_1 \rightarrow \Gamma_5$ |
| 15411 | | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_1 \rightarrow \Gamma_4$ |
| ${}^5D_1 \rightarrow {}^7F_5$ | 15437 | | | |
| | 15454 | | | |
| | 15478 | | | |
| | 15493 | | | |
| | 15511 | | | |
| ${}^5D_0 \rightarrow {}^7F_2$ | 15938 | vibronic | | |
| ${}^5D_1 \rightarrow {}^7F_4$ | 16008 | ED $\pi, \text{MD } \sigma$ | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| | 16033 | ED $\sigma, \text{MD } \pi$ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| | 16042 | ED $\sigma, \text{MD } \pi$ | $\Gamma_{3,4} \rightarrow \Gamma_2$ | $\Gamma_5 \rightarrow \Gamma_4$ |
| | 16116 | ED $\sigma, \text{MD } \pi$ | $\Gamma_{3,4} \rightarrow \Gamma_2$ | $\Gamma_5 \rightarrow \Gamma_3$ |
| ${}^5D_0 \rightarrow {}^7F_2$ | 16120 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $(\Gamma_1 \rightarrow \Gamma_3)$ |
| ${}^5D_1 \rightarrow {}^7F_4$ | 16138 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_2 \rightarrow \Gamma_3$ |
| | 16149 | ED $\sigma, \text{MD } \pi$ | $\Gamma_{3,4} \rightarrow \Gamma_1$ | $\Gamma_5 \rightarrow \Gamma_2$ |
| | 16206 | ED $\pi, \text{MD } \sigma$ | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| | 16230 | ED $\sigma, \text{MD } \pi$ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| ${}^5D_0 \rightarrow {}^7F_2$ | 16293 | ED σ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_1 \rightarrow \Gamma_5$ |

(continued overleaf)

TABLE II. (continued)

| Transition | $\bar{\nu}$ (cm ⁻¹) | Polarisation and mechanism | Identification | |
|-------------------------------|---------------------------------|----------------------------|---|-------------------------------------|
| | | | S_4 | D_{2d} |
| | 16379 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_1 \rightarrow \Gamma_4$ |
| ${}^5D_1 \rightarrow {}^7F_4$ | 16413 | ED σ , MD π | $\Gamma_{3,4} \rightarrow \Gamma_1$ | $\Gamma_5 \rightarrow \Gamma_1$ |
| ${}^5D_0 \rightarrow {}^7F_1$ | 16840 | MD σ | $\Gamma_1 \rightarrow \Gamma_1$ | $\Gamma_1 \rightarrow \Gamma_2$ |
| | 16935 | MD π | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_1 \rightarrow \Gamma_5$ |
| ${}^5D_1 \rightarrow {}^7F_3$ | 16982 | ED σ , MD π | $\Gamma_{3,4} \rightarrow \Gamma_2$ | $\Gamma_5 \rightarrow \Gamma_3$ |
| | 17002 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_2 \rightarrow \Gamma_3$ |
| | 17067 | ED π , MD σ | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| | 17089 | ED σ , MD π | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| | 17117 | ED σ , MD π | $\Gamma_{3,4} \rightarrow \Gamma_1$ | $\Gamma_5 \rightarrow \Gamma_2$ |
| | 17146 | ED π , MD σ | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| | 17159 | ED σ , MD π | $\Gamma_{3,4} \rightarrow \Gamma_2$ | $\Gamma_5 \rightarrow \Gamma_4$ |
| | 17169 | ED σ , MD π | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| | 17183 | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | ($\Gamma_2 \rightarrow \Gamma_4$) |
| | ${}^5D_1 \rightarrow {}^7F_2$ | 17844 | MD π | $\Gamma_{3,4} \rightarrow \Gamma_1$ |
| 17868 | | MD σ | $\Gamma_1 \rightarrow \Gamma_1$ | $\Gamma_2 \rightarrow \Gamma_1$ |
| 17891 | | ED π | $\Gamma_1 \rightarrow \Gamma_2$ | $\Gamma_2 \rightarrow \Gamma_3$ |
| 18042 | | MD σ | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| 18064 | | MD π | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| 18129 | | MD π | $\Gamma_{3,4} \rightarrow \Gamma_2$ | $\Gamma_5 \rightarrow \Gamma_4$ |
| ${}^5D_1 \rightarrow {}^7F_1$ | | 18589 | ED σ , MD π | $\Gamma_{3,4} \rightarrow \Gamma_1$ |
| | 18601 | MD σ | $\Gamma_1 \rightarrow \Gamma_1$ | ($\Gamma_2 \rightarrow \Gamma_2$) |
| | 18685 | ED π , MD σ | $\Gamma_{3,4} \rightarrow \Gamma_{3,4}$ | $\Gamma_5 \rightarrow \Gamma_5$ |
| | 18709 | MD π , ED σ | $\Gamma_1 \rightarrow \Gamma_{3,4}$ | $\Gamma_2 \rightarrow \Gamma_5$ |
| ${}^5D_1 \rightarrow {}^7F_0$ | 19019 | MD π | $\Gamma_{3,4} \rightarrow \Gamma_1$ | $\Gamma_5 \rightarrow \Gamma_1$ |
| | 19040 | MD σ | $\Gamma_1 \rightarrow \Gamma_1$ | $\Gamma_2 \rightarrow \Gamma_1$ |

a corresponding Γ_1 to Γ_2 (in S_4) transition, situated 21 cm⁻¹ higher in energy, but this is not observed. As explanation one can suggest that this transition corresponds to the forbidden $\Gamma_2 \rightarrow \Gamma_4$ in D_{2d} .

The third $\Gamma_{3,4}$ to Γ_1 line should appear at about 15935 cm⁻¹, but is superposed on the vibronic transition at that wavenumber.

Region 14900–15300 cm⁻¹ (Fig. 1c) $\rightarrow {}^7F_5$

This region corresponds to the ${}^5D_1 \rightarrow {}^7F_5$ transition. The identification and position of Stark levels is hard to get: no comparison is possible since the ${}^5D_0 \rightarrow {}^7F_5$ transition is not observed. Moreover, the signal to noise ratio is very poor.

An attempt to assign the peaks is given in Table II, mainly based on the previous analysis and on the

results of the crystal field calculation that simulates the presence of the Stark levels in this region.

The result of the identification of the electronic transitions is given in Table II. The experimental energy levels are given in Table III and Fig. 3.

Crystal Field Parametrisation

Due to the high degeneracy (3003) of the $4f^6$ configuration, it is not practicable to diagonalize the full secular determinant, even if it can be reduced to three submatrices for the S_4 and D_{2d} symmetries. As the ground septet is well isolated and there are no other multiplets with that same multiplicity, the $|{}^7F_J\rangle$ wavefunctions have a quite pure 7F character (90 to 95%) and the J -mixing operates only within the multiplet. The calculation of the crystal field

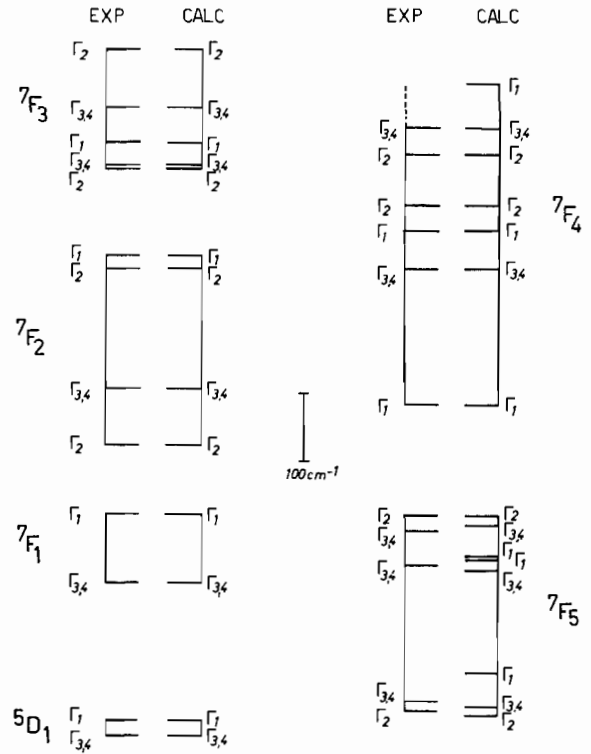
TABLE III. Experimental and Calculated Energy Levels of Eu^{3+} in LiYF_4 .

| Multiplet | $\bar{\nu}_{\text{exp}}$ (cm^{-1}) | $\bar{\nu}_{\text{calc}}$ (cm^{-1}) | Symmetry assignment | |
|-----------|---|--|---------------------|----------------|
| | | | D_{2d} | S_4 |
| 7F_0 | 0 | 0 | Γ_1 | Γ_1 |
| 7F_1 | 334 | 335 | Γ_5 | $\Gamma_{3,4}$ |
| | 430 | 429 | Γ_2 | Γ_1 |
| 7F_2 | 891 | 888 | Γ_4 | Γ_2 |
| | 976 | 975 | Γ_5 | $\Gamma_{3,4}$ |
| | 1150 | 1150 | Γ_3 | Γ_2 |
| | 1172 | 1177 | Γ_1 | Γ_1 |
| | | | | |
| 7F_3 | 1859 | 1862 | Γ_4 | Γ_2 |
| | 1873 | 1872 | Γ_5 | $\Gamma_{3,4}$ |
| | 1903 | 1899 | Γ_2 | Γ_1 |
| | 1951 | 1952 | Γ_5 | $\Gamma_{3,4}$ |
| | 2038 | 2038 | Γ_3 | Γ_2 |
| | | | | |
| 7F_4 | 2606 | 2608 | Γ_1 | Γ_1 |
| | 2812 | 2813 | Γ_5 | $\Gamma_{3,4}$ |
| | 2870 | 2873 | Γ_2 | Γ_1 |
| | 2905 | 2903 | Γ_3 | Γ_2 |
| | 2978 | 2977 | Γ_4 | Γ_2 |
| | 3013 | 3010 | Γ_5 | $\Gamma_{3,4}$ |
| | — | 3074 | Γ_1 | Γ_1 |
| | | | | |
| | | | | |
| 7F_5 | 3795 | 3787 | Γ_3 | Γ_2 |
| | 3807 | 3799 | Γ_5 | $\Gamma_{3,4}$ |
| | | 3847 | Γ_2 | Γ_1 |
| | 3998 | 3995 | Γ_5 | $\Gamma_{3,4}$ |
| | | 4011 | Γ_1 | Γ_1 |
| | | 4014 | Γ_2 | Γ_1 |
| | 4050 | 4059 | Γ_5 | $\Gamma_{3,4}$ |
| | 4070 | 4074 | Γ_4 | Γ_2 |
| 5D_0 | (17270) | 17257 ^a | Γ_1 | Γ_1 |
| 5D_1 | 19019 | 19012 ^a | Γ_5 | $\Gamma_{3,4}$ |
| | 19040 | 19046 ^a | Γ_2 | Γ_1 |

^aCalculated from the extended basis.

parameters can be performed accurately on this strongly reduced basis (49×49) when the calculated barycenters are adjusted to the experimental ones.

The crystal field potentials for D_{2d} and S_4 symmetries are:

Fig. 3. Energy diagram of $\text{LiYF}_4/\text{Eu}^{3+}$ in a S_4 symmetry.

$$D_{2d}: H^{\text{even}} = B_0^2 C_0^2 + B_0^4 C_0^4 + B_4^4 (C_4^4 + C_{-4}^4) \\ + B_0^6 C_0^6 + B_4^6 (C_4^6 + C_{-4}^6)$$

$$H^{\text{odd}} = i B_2^3 (C_2^3 - C_{-2}^3) + i B_2^5 (C_2^5 - C_{-2}^5) \\ + i B_2^7 (C_2^7 - C_{-2}^7) + i B_6^7 (C_6^7 - C_{-6}^7)$$

$$S_4: H^{\text{even}} = H_{D_{2d}}^{\text{even}} + i B_4^4 (C_4^4 - C_{-4}^4) + i B_4^6 (C_4^6 - C_{-4}^6)$$

$$H^{\text{odd}} = H_{D_{2d}}^{\text{odd}} + B_2^3 (C_2^3 + C_{-2}^3) + B_2^5 (C_2^5 + C_{-2}^5) \\ + B_2^7 (C_2^7 + C_{-2}^7) + B_6^7 (C_6^7 + C_{-6}^7)$$

The number of even c.f.p. for S_4 can be reduced to six if $i B_4^4$ is set to zero by an appropriate choice of the reference axis system.

Different c.f.p. determinations have been performed for this crystalline matrix, with different rare earth doping ions, and including or not the imaginary $i B_4^4$ parameter. Results are summarized in ref. 2. For the Eu^{3+} case we considered values extrapolated from the literature as starting parameters. These parameters were slightly modified in order to simulate more correctly the observed splittings: B_0^2 for the 7F_1 splitting, B_0^4 and B_4^4 for 7F_2 and other parameters for 7F_3 and 7F_4 .

Therefore, the final refining procedure runs rapidly towards a low r.m.s. (3 cm^{-1}) with a correct

assignment to the irreducible representations. The c.f.p. values are:

$$B_0^2: 349 (\pm 3) \text{ cm}^{-1}$$

$$B_0^4: -728 (\pm 4) \text{ cm}^{-1}$$

$$B_4^4: -919 (\pm 3) \text{ cm}^{-1}$$

$$B_0^6: -35 (\pm 6) \text{ cm}^{-1}$$

$$B_4^6: -790 (\pm 4) \text{ cm}^{-1}$$

$$iB_4^6: 216 (\pm 9) \text{ cm}^{-1}$$

The signs of B_4^4 and B_4^6 are reversed from all other calculations. This feature does not modify at all the energy level positions, but permutes the B_1 and B_2 irreducible representations. This has to be related to the relative weakness of certain transitions, which are allowed when the symmetry is S_4 but forbidden if the approximative D_{2d} symmetry is considered.

Moreover, it has been shown elsewhere that some configuration truncation [9, 10] could be considered if one wants to simulate correctly the excited 5D_0 , 5D_1 and 5D_2 level positions together with 7F_J , and to derive the complete wave functions associated with these levels. By using the calculated c.f.p. values given above (with iB_4^6 set to zero), this procedure allows an estimation of the free ion parameters. The derived values are: $E_0 = 2880 \text{ cm}^{-1}$, $E_1 = 5544 \text{ cm}^{-1}$, $E_2 = 24.83 \text{ cm}^{-1}$, $E_3 = 585 \text{ cm}^{-1}$, $\alpha = 20 \text{ cm}^{-1}$, $\beta = -640 \text{ cm}^{-1}$, $\gamma = 1750 \text{ cm}^{-1}$ and $\xi = 1285 \text{ cm}^{-1}$.

Conclusion

This paper reports a spectroscopic study on the LiYF_4 crystal, doped with the Eu^{3+} ion. Whereas several studies have been published on the LiYF_4 doped with other ions [2, 12–15], this is to our knowledge the first time that Eu^{3+} -doped crystals were grown with size and quality adequate for optical measurements.

In this paper the fluorescence spectrum has been analyzed and accurately described by a set of parameters whose order of magnitude and sign fit rather well in the list of those recently reported in the review by Morrison and Leavitt [2].

Nevertheless, the particular case of Eu^{3+} gives more precision about the sign of some crystal field parameters.

The reverse of the sign of the B_4^4 and B_4^6 parameters with respect to those given by other authors [1, 2], does not modify the energy level scheme but permutes the B_1 and B_2 crystal field representations. The wave functions associated with these levels also

show inversions in the sign of some of their components. The magneto-optical measurements should help us in solving this problem.

Our interest for the $\text{LiYF}_4/\text{Eu}^{3+}$ crystal is mainly motivated by its parentage with the $\text{KY}_3\text{F}_{10}/\text{Eu}^{3+}$ crystal. This is one of the few examples where the phase diagram allows that a same ion (Eu^{3+}) complexed with a same ligand (F^-) can be studied in two different site symmetries namely D_{2d} for LiYF_4 and C_{4v} for KY_3F_{10} . A complete study of the $\text{KY}_3\text{F}_{10}/\text{Eu}^{3+}$ has been published [16–18].

A prospective comparison between the magneto-optical spectra of both compounds allows us to state that the sign inversion predicted theoretically in previous papers between the C_{4v} and D_{2d} symmetry [3, 19] is indeed found experimentally.

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